



ISSN: 3049-382X (Online)

**Journal of Recent Trends of Electrical Engineering**

contents available at: <https://www.swamivivekanandauniversity.ac.in/jrtee/>

# Dynamic State Estimation for Power System Protection: Methods, Challenges, and Emerging Directions

Suvraujjal Dutta , MAKAUT, Haringhata, Nadia, India

Sandip Chanda, GKCIET, Malda

Alok Kumar Shrivastav ,JIS College of Engineering ,Kalyani

Abhinandan De, IEST, Shibpur

---

## Abstract

*Dynamic State Estimation (DSE) has emerged as a transformative technology for enhancing the dependability, security, and resilience of modern power system protection. With growing penetration of renewable energy, reduced system inertia, and increased dependence on fast-acting digital protection schemes, traditional quasi-static estimation methods are no longer sufficient. This paper presents a comprehensive and original overview of DSE in the context of power system protection. Fundamental models, estimation algorithms, measurement technologies, and practical implementation challenges are discussed. Special emphasis is placed on the interactions between DSE and protection functions such as fault detection, classification, adaptive relay settings, state prediction, and cyber-physical resilience. The paper concludes with emerging trends including machine-learning-enhanced DSE, distributed estimation for wide-area protection, and high-speed phasor-based dynamic monitoring.*

---

**Keywords :** *Dynamic State Estimation (DSE), Power System Protection, Fault Detection, Adaptive Protection, Cyber-Physical Resilience, Renewable Integration, Machine Learning, Wide-Area Monitoring, Phasor Measurement Units (PMUs), Real-Time Grid Monitoring*

## 1. Introduction

Power systems are becoming increasingly dynamic due to renewable generation, electronically interfaced resources, variable loads, and complex grid topology. Protection systems,

responsible for detecting and clearing faults, must operate reliably despite these rapid and uncertain dynamics.

Traditional protection and state estimation rely heavily on *steady-state* assumptions, such as balanced sinusoidal waveforms and slowly varying operating conditions. However, disturbances now evolve on millisecond timeframes, and system responses are highly nonlinear. As a result, **Dynamic State Estimation (DSE)** has gained attention for:

capturing real-time transient behaviour,

improving situational awareness,

enhancing fault detection and protection logic,

enabling adaptive relay settings,

supporting resilient operation under cyber-attacks.

DSE leverages dynamic models and high-frequency measurements (e.g., synchrophasors, traveling wave sensors) to estimate rapidly changing electrical variables such as generator rotor angles, bus voltage magnitudes, frequency, and line states. Unlike static state estimation (SE), which estimates states only at pre-fault or steady conditions, DSE monitors the system *continuously* and *during* disturbances.

This paper reviews the state-of-the-art in DSE for power system protection, focusing on algorithms, models, and their integration into real protection schemes.

## 2. Dynamic Modelling for Power System Protection

### 2.1 State-Space Representation

Most DSE frameworks rely on a discrete-time nonlinear state-space model:

$$x_{k+1} = f(x_k, u_k) + w_k$$

$$y_k = h(x_k) + v_k$$

Where:

$x_k$ : states such as rotor angle, speed, internal generator voltage, line currents, bus voltages

$u_k$ : mechanical input power, excitation signals, or control inputs

$y_k$ : PMU or relay measurements

$w_k, v_k$ : process and measurement noise

Key protective states include:

generator dynamic states ( $\delta, \omega$ ),

line current dynamics,

protection zone boundaries,

voltage and frequency trajectory under disturbances.

## 2.2 Power System Dynamic Models

### 2.2.1 Synchronous Generator Model

A common DSE generator model is the second-order swing equation:

$$\begin{aligned}\delta_{k+1} &= \delta_k + \Delta t \cdot \omega_k \\ \omega_{k+1} &= \omega_k + \Delta t \left( \frac{P_m - P_e}{M} - \frac{D}{M} \omega_k \right)\end{aligned}$$

### 2.2.2 Transmission Line Dynamic Model

Differential equations for line currents:

$$\frac{di}{dt} = \frac{1}{L}(v_s - Ri - v_r)$$

Discretized for DSE:

$$i_{k+1} = \alpha i_k + \beta(v_{s,k} - v_{r,k})$$

These models form the basis for protection-oriented DSE.

## 3. Dynamic State Estimation Algorithms in Protection

### 3.1 Extended Kalman Filter (EKF)

The EKF linearizes nonlinear dynamics to update protection system states:

Prediction:

$$\hat{x}_{k+1|k} = f(\hat{x}_{k|k})$$

$$P_{k+1|k} = A_k P_{k|k} A_k^T + Q_k$$

Update:

$$K_k = P_{k|k-1} C_k^T (C_k P_{k|k-1} C_k^T + R_k)^{-1}$$

$$\hat{x}_{k|k} = \hat{x}_{k|k-1} + K_k (y_k - h(\hat{x}_{k|k-1}))$$

EKF is widely used but may struggle with severe nonlinearities during faults.

### 3.2 Unscented Kalman Filter (UKF)

The UKF uses sigma points, offering superior estimation under fast transients:

no linearization errors  
better for protection under saturation, switching transients, and nonlinear loads

UKF is increasingly preferred for generator and transmission line protection.

### 3.3 Particle Filters (PF)

PFs approximate the state distribution using sample particles:

$$x_k^{(i)} \sim p(x_k | x_{k-1}^{(i)})$$

$$w_k^{(i)} \propto p(y_k | x_k^{(i)})$$

Advantages for protection:

handles nonlinear, non-Gaussian conditions  
robust to disturbances caused by faults and switching

PFs are ideal for fault classification, arc fault detection, and cyber-physical anomalies.

### 3.4 Moving Horizon Estimation (MHE)

MHE solves a constrained optimization problem over a moving time window:

$$\hat{X}_k = \arg \min \left( \|x_{k-N} - \hat{x}\|_{P^{-1}}^2 + \sum \|w\|_{Q^{-1}}^2 + \sum \|y - h(x)\|_{R^{-1}}^2 \right)$$

Benefits for protection:

- incorporates physical and operational constraints
- effective for systems with limited or uncertain measurements
- supports adaptive relay settings

## 4. Measurement Technologies for DSE in Protection

### 4.1 Phasor Measurement Units (PMUs)

PMUs provide synchronized voltage and current phasors at 30–240 samples per second. They enable:

- wide-area protection,
- dynamic monitoring of line angles,
- real-time assessment of transient stability.

### 4.2 High-Speed Fault Recorders

Capture high-frequency transients (>1 kHz), critical for:

- traveling-wave protection
- transient-based DSE
- detecting incipient equipment failures

### 4.3 Distributed sensors and merging units

In modern power systems, distributed sensors and merging units (MUs) play a key role in digitizing and transmitting substation measurements.

#### Distributed Sensors

These are sensors (like current transformers (CTs) and voltage transformers (VTs)) that measure electrical quantities directly at the primary equipment.

They provide high-accuracy, time-stamped data for protection, control, and monitoring purposes.

Advantages:

- Reduced wiring complexity
- Easier integration with digital systems

Better signal quality

### **Merging Units (MUs)**

A merging unit collects analog measurements from multiple sensors.

It converts these analog signals into digital samples.

It then sends them over the process bus using the IEC 61850-9-2 standard.

### **IEC 61850 Process Bus**

IEC 61850 is an international standard for substation automation.

The process bus is the network that connects MUs to protection and control relays.

Key feature: streaming of time-stamped measurements.

Relays receive synchronized voltage and current samples.

Time stamps ensure accurate phasor calculations and fault detection.

Benefits:

Faster protection response

Reduced need for copper wiring

Easier system reconfiguration

## **5. Applications of DSE in Power System Protection**

### **5.1 Fault Detection and Classification**

DSE enhances fault detection by observing deviations in dynamic states:

sudden changes in rotor speed

abrupt voltage angle jumps

abnormal line current dynamics

DSE can classify:

SLG, LLG, LLL, and LLLG faults

high impedance faults

series/line breaker failures

evolving multi-stage faults

## 5.2 Adaptive Protection

Traditional relay settings are static; DSE enables adaptive adjustments based on real-time states:

distance relay zone adjustments

overcurrent pickup value updating

directional element reliability under reverse flows

## 5.3 Transient Stability Assessment

DSE provides real-time estimates of rotor angle differences:

$$\Delta\delta = \delta_i - \delta_j$$

Used to:

predict instability

trigger controlled islanding

enable emergency load shedding

## 5.4 Wide-Area Protection Schemes

DSE improves wide-area protection by:

detecting inter-area oscillations

identifying cascading failures early

distinguishing false data injection attacks

## 5.5 Cyber-Physical Attack Mitigation

DSE can detect inconsistencies between:

system dynamics

measurement trajectories

This allows detection of:

GPS spoofing  
relay setting manipulation  
false PMU data injection

## 6. Challenges in Implementing DSE for Protection

### 6.1 Nonlinear and Fast Transient Behaviour

Faults cause highly nonlinear transient conditions difficult for Kalman filters.

### 6.2 Measurement Latency and Noise

PMUs have delays (20–80 ms), which affect protective speed requirements.

### 6.3 Model Uncertainties

Protection devices often rely on simplified models that may not capture dynamics of:  
inverter-based resources  
dynamic loads  
protective switching events

### 6.4 Computation and Real-Time Requirements

Protection operation requires millisecond-level response, challenging for:  
particle filters  
large MHE problems

### 6.5 Cybersecurity Threats

Cybersecurity Threats:

Cybersecurity threats refer to actions or events that compromise the confidentiality, integrity, or availability of digital systems. In modern power grids and industrial systems, these threats can target:

Control systems (SCADA, relays, PLCs)  
Communication networks (process bus, station bus)  
Distributed sensors and merging units

## 1. Types of Cybersecurity Threats

### A. Malware

Malicious software designed to disrupt, damage, or gain unauthorized access.

Examples: viruses, worms, ransomware, trojans.

Impact: system downtime, data theft, or manipulation of measurements.

### B. Phishing & Social Engineering

Attackers trick personnel into revealing credentials or executing malicious commands.

Impact: unauthorized system access.

### C. Denial of Service (DoS) / Distributed DoS

Overloads network or devices, preventing legitimate communication.

In power systems: relays or control centers may fail to receive critical measurements.

#### D. Man-in-the-Middle (MitM) Attacks

Interception or modification of communication between devices.

Example: altering sensor data between merging units and relays.

#### E. Insider Threats

Authorized personnel intentionally or accidentally compromise security.

Could involve misconfiguration, sabotage, or theft of sensitive information.

#### F. Advanced Persistent Threats (APTs)

Sophisticated, long-term attacks by organized groups.

Goal: silently manipulate or monitor systems over time.

Examples: Stuxnet (targeted industrial control systems)

### 2. Threat Vectors in Power Systems

**Process bus (IEC 61850):** digital measurement streams could be spoofed or delayed.

**Control center networks:** SCADA or EMS systems vulnerable to remote exploitation.

**Field devices:** smart meters, distributed sensors, or merging units could be compromised.

**Communication protocols:** unencrypted or unauthenticated messages can be intercepted or altered.

### 3. Potential Consequences

Incorrect relay operation → false trips or failure to trip

Grid instability or blackouts

Equipment damage

Data theft or privacy violations

### 4. Mitigation Strategies

**Encryption & authentication:** secure communication between devices.

**Network segmentation:** separate critical control networks from IT networks.

**Regular software updates & patching:** reduce vulnerability to malware.

**Intrusion detection & monitoring:** detect unusual patterns or anomalies.

**Access control & personnel training:** minimize insider threats.

**Redundancy & fail-safe designs:** ensure reliability even under attack.

### 7. Emerging Trends and Future Directions

#### 7.1 Machine Learning–Enhanced DSE

Neural networks improve prediction accuracy for unknown or complex dynamics:

$$x_{k+1} = f_{\text{physics}}(x_k) + g_{\theta}(x_k)$$

#### 7.2 Distributed DSE for Wide-Area Protection

Agents collaborate to estimate states without a central controller, improving reliability under communication failures.

### 7.3 DSE for Systems with High Renewable Penetration

Inverter-based resources exhibit fast, non-sinusoidal dynamics requiring advanced nonlinear estimation.

### 7.4 Quantum and High-Performance Computing for Protection

Modern and future protection systems in power grids are exploring advanced computing technologies to enhance speed, accuracy, and reliability.

#### Background

Protective relays monitor the electrical system and make decisions (like tripping a breaker) when faults occur. Traditional relays operate on millisecond timescales, using methods like: Overcurrent, distance, differential protection

Phasor or numerical calculations

However, future grids are becoming more complex due to:

Distributed generation (solar, wind)

Micro grids

Dynamic loads

This requires faster and more precise computations, sometimes at microsecond granularity.

#### Dynamic State Estimation (DSE)

DSE is an advanced method to estimate the real-time state of the power system, including voltages, currents, and internal states of generators.

Conventional DSE can be computationally intensive, especially for large networks.

Faster computation enables protection relays to respond almost instantaneously to faults or disturbances.

#### High-Performance Computing (HPC) and Quantum Computing

##### High-Performance Computing (HPC)

Uses parallel processing, GPUs, or specialized accelerators to solve complex calculations quickly.

Benefits for protection:

Faster DSE computation

Ability to handle large networks in real time

Improved situational awareness and predictive protection

##### Quantum Computing

Quantum algorithms can theoretically solve certain optimization and state estimation problems exponentially faster than classical computers.

In protection:

Quantum solvers could perform DSE in microseconds, enabling ultra-fast fault detection and system stabilization.

#### Microsecond-Scale Relays

Current digital relays: respond in milliseconds.

Future relays using HPC or quantum solvers: respond in microseconds.

Implications:

Extremely fast fault isolation

Reduced stress on grid components  
Better integration of renewable and dynamic resources

## 8. Conclusion

Dynamic State Estimation (DSE) provides an essential foundation for next-generation protection schemes in modern power systems. By continuously monitoring the real-time operating states of generators, transmission lines, and loads, DSE enables operators and protective devices to gain a highly accurate, system-wide situational awareness. By integrating advanced estimation algorithms—such as Kalman filters, particle filters, unscented Kalman filters, and observer-based techniques—with high-speed phasor measurement unit (PMU) data, DSE can track both the dynamic and algebraic states of the power system with unprecedented precision. The incorporation of machine-learning-enhanced models further strengthens DSE by allowing predictive analytics, anomaly detection, and adaptive protection schemes that can respond intelligently to evolving system conditions. These capabilities enable faster and more accurate fault detection, optimized relay coordination, real-time transient stability monitoring, and enhanced cyber-physical resilience against attacks or communication failures. As modern power grids continue to evolve with increasing integration of variable renewable energy sources, distributed energy resources, microgrids, and digitalized control infrastructures, the role of DSE becomes increasingly critical. Its ability to provide high-fidelity, time-synchronized state information ensures that protection systems can operate adaptively under complex, nonlinear, and uncertain conditions. Consequently, DSE is poised to serve not only as a backbone for advanced protection and control schemes but also as a key enabler of grid reliability, security, and operational stability in the future intelligent power system.

## References:

- [1] Zhao, J., Gómez-Expósito, A., Netto, M., Mili, L., Abur, A., Terzija, V., Kamwa, I., Pal, B., Singh, A.K., Qi, J., Huang, Z., Meliopoulos, A.P. “Power System Dynamic State Estimation: Motivations, Definitions, Methodologies and Future Work.” *IEEE Transactions on Power Systems*, 34(4), pp. 3188–3198, 2019.
- [2] Liu, Y., Singh, A. K., Zhao, J., Meliopoulos, A. P., Pal, B., Ariff, M.A.M., Van Cutsem, T., Glavic, M., Huang, Z., Kamwa, I., Mili, L., Mir, A. S., Taha, A., Terzija, V., Yu, S. “Dynamic State Estimation for Power System Control and Protection.” *IEEE Transactions on Power Systems*, 36(6), pp. 5909–5921, 2021.
- [3] Zhao, J., Netto, M., Huang, Z., Yu, S., Gómez-Expósito, A., Wang, S., Kamwa, I., Akhlaghi, S., Mili, L., Terzija, V., Meliopoulos, A. P., Pal, B., Bi, T., Rouhani, A. “Roles of Dynamic State Estimation in Power System Modeling, Monitoring and Operation.” *IEEE Transactions on Power Systems*, 36(3), pp. 2462–2472, 2021.
- [4] “Dynamic State Estimation in Power Systems.” Hamed Tebianian, M.Eng. Thesis, Memorial University, 2014.
- [5] “Static and Dynamic State Estimation of Power Systems.” Zhaoyang Jin, PhD Thesis, The University of Manchester, 2017.
- [6] “A survey on recent advances on dynamic state estimation for power systems.” B. Qu, D. Peng, Y. Shen, L. Zou, B. Shen. *International Journal of Electrical Power & Energy Systems* (2024) (or similar journal).

- 
- 
- [7] “Dynamic state estimation for power system control and protection” — preprint / technical report (2020).
  - [8] Nadeem, M., Nugroho, S. A., & Taha, A. F. “Dynamic State Estimation of Nonlinear Differential Algebraic Equation Models of Power Networks.” *IEEE Transactions on Power Systems*, (in press / 2022).
  - [9] Aryasomyajula, V. A., Gatsis, N., & Taha, A. F. “Power System Dynamic State Estimation Based on Discretized Nonlinear Differential Algebraic Equation Models.” 2022 North American Power Symposium (NAPS), 2022.
  - [10] “Observers for Differential Algebraic Equation Models of Power Networks: Jointly Estimating Dynamic and Algebraic States.” Sebastian Nugroho, Ahmad Taha, Nikolaos Gatsis, Junbo Zhao. *IEEE Transactions on Control of Network Systems*, 2022.
  - [11] “Robust Dynamic State Estimation of Multi-Machine Power Networks with Solar Farms and Dynamic Loads.” Muhammad Nadeem & Ahmad F. Taha. arXiv preprint, 2022.
  - [12] Katanic, M., Lygeros, J., & Hug, G. “Recursive Dynamic State Estimation for Power Systems with an Incomplete Nonlinear DAE Model.” arXiv preprint, 2023.
  - [13] “Data-resilient dynamic state estimation in power systems under communication constraints.” (2025) — addresses communication-induced data loss in microgrids via machine-learning regression-based DSE.
  - [14] “A Robust Dynamic State Estimation Method for Power Systems Considering Maximum Correlation Entropy and Quadratic Function.” T. Chen, 2024. “A new robust dynamic state estimation approach for power systems.” T. Chen, 2024.
  - [15] “Robust Dynamic State Estimation of Power System With Measurement Outliers Based on Parameterized Analytical Cubature Kalman Filter (PACKF).” (2025) “Resilient Dynamic State Estimation for Power System with Outliers and Non-Gaussian Noise.” Z. Gao et al., 2025.
  - [16] “Deep Generative Model-Aided Power System Dynamic State Estimation and Reconstruction with Unknown Control Inputs or Data Distributions.” Jianhua Pei, Ping Wang, Jingyu Wang, Dongyuan Shi, 2025.
  - [17] “Deep Learning-Based Dynamic State Estimation for Frequency Stability Monitoring in Power Systems with High Penetration of Renewable Generation.” Said Ćosić and István Vokony, EEPES’23, 2023.
  - [18] “Dynamic state estimator for power systems modeled by constrained DAEs using an active-set UKF framework.” (2025) — extension of UKF to DAE constraints.
  - [19] “Dynamic State Estimation of Electric Power Systems Using Kalman Filtering Techniques.” (2025) — a broad overview of KF applications for DSE.
  - [20] “A Comprehensive Review of Hybrid State Estimation in Power Systems: Challenges, Opportunities and Prospects.” (2024) — though focused on state estimation broadly, includes hybrid (static + dynamic) SE discussions relevant to DSE.
  - [21] “A robust iterated Extended Kalman Filter for power system dynamic state estimation.” Zhao, J., Netto, M., Mili, L., 2016. (as referenced in [2])
  - [22] “Local and wide-area PMU-based decentralized dynamic state estimation in multi-machine power systems.” Ghahremani, E. & Kamwa, I., *IEEE Trans. Power Systems*, 2016. (as referenced in [8])
  - [23] “Dynamic state estimation of a synchronous machine using PMU data: A comparative study.” N. Zhou, D. Meng, Z. Huang & G. Welch. *IEEE Trans. Smart Grid*, 2015. (as referenced in [8])

- [24] “Application of Ensemble Kalman Filter in Power System State Tracking and Sensitivity Analysis.” Y. Li, Z. Huang, N. Zhou, B. Lee, R. Diao, P. Du, PES T&D 2012. (as referenced in [8])
- [25] “Deterministic dynamic state estimation–based optimal load frequency control for interconnected power systems using unknown input observer.” Haes Alhelou, H., Golshan, M. E. H., Hatziargyriou, N. D., IEEE Trans. Smart Grid, 2020. (as referenced in [8])
- [26] “Higher order sliding mode observers and estimation of synchronous machines.” G. Rinaldi & A. Ferrara, IEEE Trans. Power Systems, 2017. (as referenced in [8])
- [27] “Correlation-aided robust decentralized dynamic state estimation of power systems with unknown control inputs.” J. Zhao, Z. Zheng, S. Wang, R. Huang, T. Bi, L. Mili, Z. Huang; IEEE Trans. Power Systems, 2019/2020. (as referenced in [2],[9])
- [28] “Nonlinear model reduction in power systems by balancing empirical controllability and observability covariances.” J. Qi, J. Wang, H. Liu, A. D. Dimitrovski; IEEE Trans. Power Systems, 2017. (relevant for model simplification and DSE scalability)